

# **Downlink and Uplink Channel Modeling in OFDM/A system**

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## ■ Problem statement

- **SINR models of a MS can be different between downlink and uplink channels in OFDM/A system**
  - Downlink and uplink interference models are asynchronous
- **Downlink and uplink service requirements can be quite different in the next generation communications systems**

## ■ Objective

- **Mathematical channel models for OFDM/A system are required to guarantee the required QoS level or link quality**
- **We introduce downlink and uplink channel models of OFDM/A system**
  - Using geometrical method
  - Taking into consideration inter-cell interferences

## *Assumption*

- **System model of IEEE 802.16e**
- **One-tier cell structure**
- **Large-scale fading**
  - **Propagation loss and shadowing**
- **Uniformly distributed mobile stations**
- **Frequency reuse of one**
- **No intra-cell interference**
- **Maximum power transmission from each BS and MS**

## Probability density functions for $R_1$ , $R_2$ and $R_3$

$$f_{R_1}(r) = \frac{2r}{r_e^2}$$

$$f_{R_2}(r) \propto \frac{r\phi}{\pi r_e^2} \propto \frac{2x}{\pi r_e^2}$$

$$f_{R_3}(r) \propto \frac{2r}{(r_e + d)^2 - (d/2)^2}$$

## Expectations of $\gamma$ -th moment

$$E[r_{b \leftrightarrow m}^{-\gamma}] = \int_{\varepsilon}^{r_e} \frac{2r^{-r+1}}{r_e^2} dr$$

$$E[r_{z \leftrightarrow m}^{-\gamma}] = \int_{d-r_e}^{d+r_e} \frac{r^{-\gamma}}{\pi r_e^2} \frac{\sqrt{4d^2 r_e^2 - (d^2 + r_e^2 - r^2)^2}}{d^2} dr$$

$$E[r_{b \leftrightarrow n}^{-\gamma}] = \int_{d/2}^{d+r_e} \frac{2r^{-\gamma+1}}{(r_e + d)^2 - (d/2)^2} dr$$

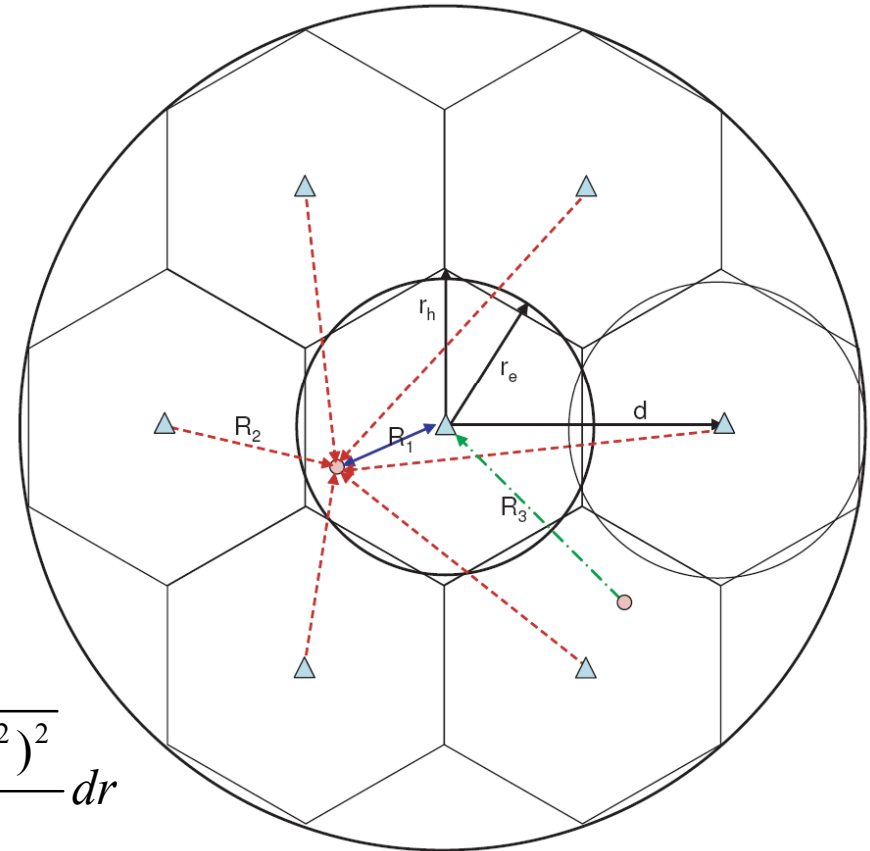


Fig 1. One inner cell and six outer cells

## ■ Expectation of log-normally distributed random variable

■ Mean of  $m_\zeta = 0$

■ Variance of  $\sigma_\zeta^2$

$$E \left[ 10^{-\zeta_{b \leftrightarrow m} / 10} \right] = 10^{-m_{\zeta_{b \leftrightarrow m}} / 10} \exp \left\{ \frac{\left( \frac{\ln 10}{10} \sigma_{\zeta_{z \rightarrow m}} \right)^2}{2} \right\}$$
$$= \exp \left\{ \frac{\left( \frac{\ln 10}{10} \sigma_{\zeta_{z \rightarrow m}} \right)^2}{2} \right\}$$

## Downlink signal to interference and noise ratio

$$\Gamma_{b \rightarrow m}^{(r)} = \left[ \frac{P_{\max, BS}^{(t)} \bar{\alpha} \int_{\varepsilon}^{r_e} \frac{2r^{-\gamma+1}}{r_e^2} dr \exp \left\{ \frac{\left( \frac{\ln 10}{10} \sigma_{\zeta_{z \rightarrow m}} \right)^2}{2} \right\}}{\frac{P_{\max, BS}^{(t)} 6 \bar{M} \bar{\alpha}^2 \theta}{360^\circ} \int_{d-r_e}^{d+r_e} \frac{r^{-\gamma}}{\pi r_e^2} \frac{\sqrt{4d^2 r_e^2 - (d^2 + r_e^2 - r^2)^2}}{d^2} dr \exp \left\{ \frac{\left( \frac{\ln 10}{10} \sigma_{\zeta_{z \rightarrow m}} \right)^2}{2} \right\} + N_o} \right]$$

$P_{\max, BS}^{(t)}$  : Maximum BS transmission power

$\bar{\alpha}$  : Downlink mean resource allocation ratio

$\bar{M}$  : Average number of active MSs in a cell

## ■ Uplink signal to interference and noise ratio

$$\Gamma_{b \rightarrow m}^{(r)} = \left[ \frac{P_{\max, BS}^{(t)} \bar{\beta} \int_{\epsilon}^{r_e} \frac{2r^{-\gamma+1}}{r_e^2} dr \exp \left\{ \frac{\left( \frac{\ln 10}{10} \sigma_{\zeta_{z \rightarrow m}} \right)^2}{2} \right\}}{\left[ \frac{P_{\max, BS}^{(t)} 6 \bar{M} \bar{\beta}^2 \theta}{360^\circ} \int_{d/2}^{d+r_e} \frac{2r^{-\gamma+1}}{(r_e + d)^2 - (d/2)^2} dr \exp \left\{ \frac{\left( \frac{\ln 10}{10} \sigma_{\zeta_{z \rightarrow m}} \right)^2}{2} \right\} + N_o \right]} \right]$$

$P_{\max, MS}^{(t)}$  : Maximum MS transmission power

$\bar{\beta}$  : Uplink mean resource allocation ratio

$\bar{M}$  : Average number of active MSs in a cell



## Parameters for numerical example

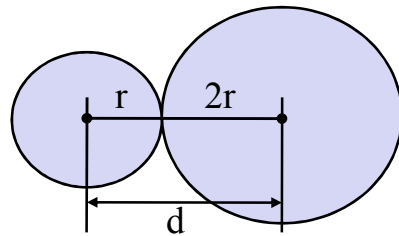
Parameter	Symbol	Value
Downlink mean resource allocation ratio	$\bar{\alpha}$	0.01
Uplink mean resource allocation ratio	$\bar{\beta}$	0.01
Power spectral density of additive white Gaussian noise	$N_o$	-174[dBm]
Transmission antenna main lobe width	$\theta$	120°
Maximum MS transmission power	$P_{\max,MS}$	30[dBm]
Maximum BS transmission power	$P_{\max,BS}$	42[dBm]
Shadowing variance	$\sigma_{\zeta}$	8[dB]
Minimum distance between an MS and a BS	$\varepsilon$	10[m]
Propagation loss factor	$\gamma$	4
Number of active MSs in a cell	$\bar{M}$	100

# Numerical results (1/2)

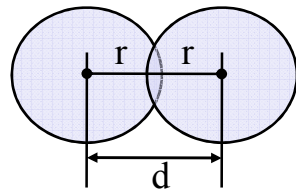
## Case 1

### A reversal of UL & DL SINR by distance of BSs

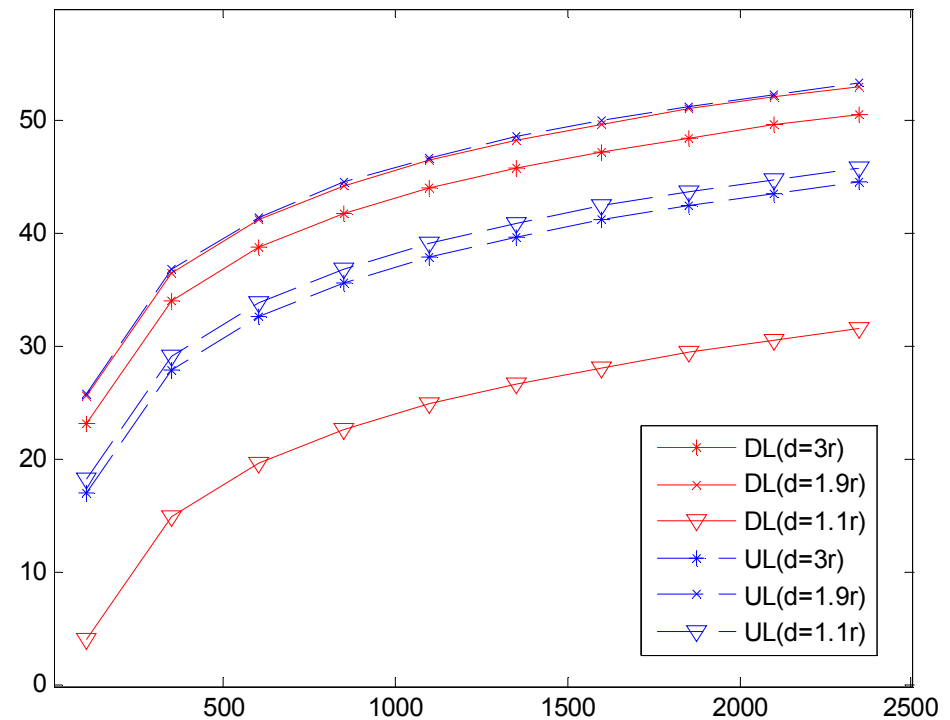
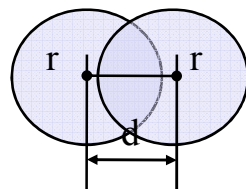
■ Star mark ( $d=3r$ )



■ Ex mark ( $d=1.9r$ )



■ Triangle mark ( $d=1.1r$ )



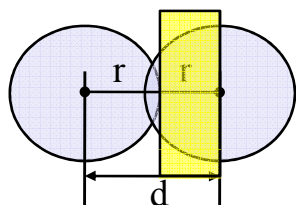
# Numerical results (2/2)

## Case 2

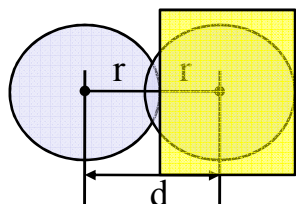
A reversal of UL & DL SINR by MSs allocation

$d=1.9r$

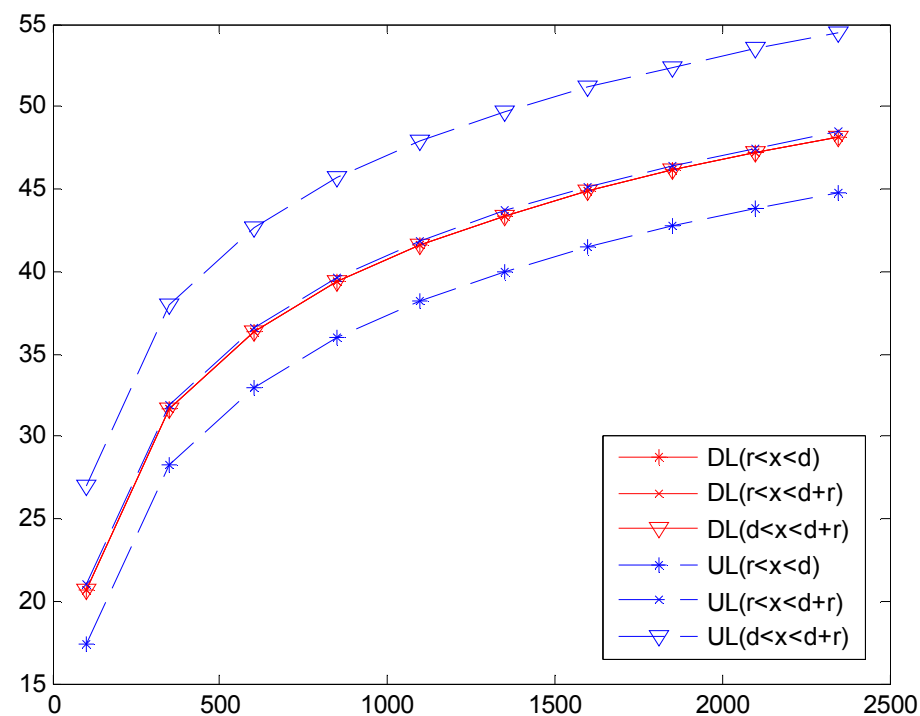
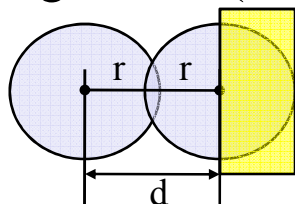
Star mark ( $r < x < d$ )



Ex mark ( $r < x < d+r$ )



Triangle mark ( $d < x < d+r$ )



# Conclusion

- **Downlink and uplink channels can be asymmetric in OFDM/A system**
  - **Cell implementation**
  - **Neighbor cell users location**
  
- **Need a new channel quality management scheme to satisfy the required service quality**

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*Thank you!*

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